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1 Input :  $G = (g_1, \dots, g_s) \in P^s$ , a Gröbner basis for  $\langle G \rangle$ ; and  $\prec$ ; a
   monomial ordering;
2 Output :  $H$  an  $s \times \ell$  matrix in which its columns are a Gröbner basis
   for  $Syz(G)$  ;
3  $B \leftarrow \{\{g_i, g_j\} : g_i, g_j \in G, i \neq j\}$ ;
4 while  $B \neq \emptyset$  do
5   | select and remove  $\{g_i, g_j\}$  from  $B$ ;
6   | if  $S(g_i, g_j) \neq 0$  then
7   |   |  $S(g_i, g_j) \leftarrow \sum_{k=1}^s q_k g_k$  using the devision algorithm;
8   |   |  $h \leftarrow (q_1, \dots, q_i - m_{ji}, \dots, q_j + m_{ij}, \dots, q_s)$  ;
9   |   | else
10  |   |   |  $h \leftarrow (0, \dots, -m_{ji}, \dots, m_{ij}, \dots, 0)$ 
11  |   |   | end
12  |   | ;
13  | end
14  |  $H \leftarrow (H \mid h^t)$ 
15 end
16 Return  $H$ 

```

**Algorithm 1:** SYZSCHREYER